



# Influence of a DLC Coating on the Temperature and Friction in a Helical Tooth Flank Contact

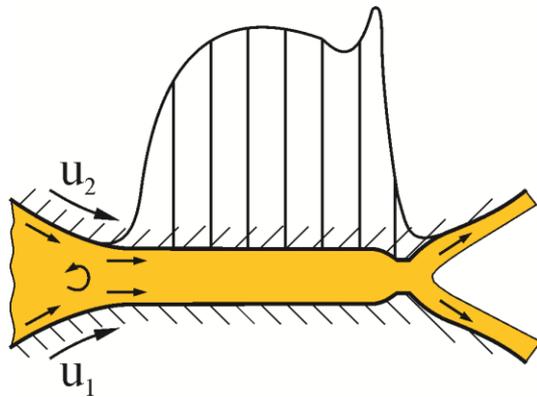
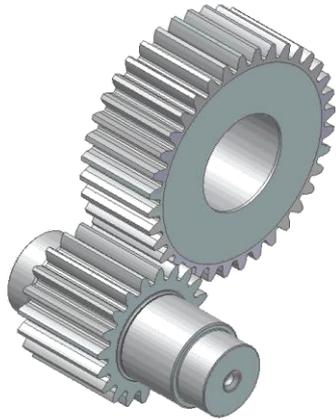
*Ronny Beilicke, Lars Bobach, Dirk Bartel*

Institute of Machine Design  
Chair of Machine Elements and Tribology  
Otto von Guericke University Magdeburg, Germany

# Content

---

- Introduction
- 3D TEHL Calculation Model
- Calculation Example
- Results
- Summary



## Tooth flank contact is characterized by

- involute tooth flank profiles including gearing corrections
- gradual meshing
- transient thermal elastohydrodynamic finite line contact
- high pressures
- high shear rates

## Contact simulation requires

- transient 3D TEHL calculation model, applied on gearing
- consideration of lubricant rheology including non-Newtonian behavior
- mixed friction approach
- temperature calculation

# Content

---

- Introduction
- 3D TEHL Calculation Model
- Calculation Example
- Results
- Summary

# 3D TEHL Calculation Model

## Calculation Model

Elastohydrodynamics

Real Gear Pair Geometry

Realistic Load Distribution

Lubricant Rheology

Rough Surfaces

Mixed Friction Conditions

Temperature Calculation

## Generalized Reynolds equation

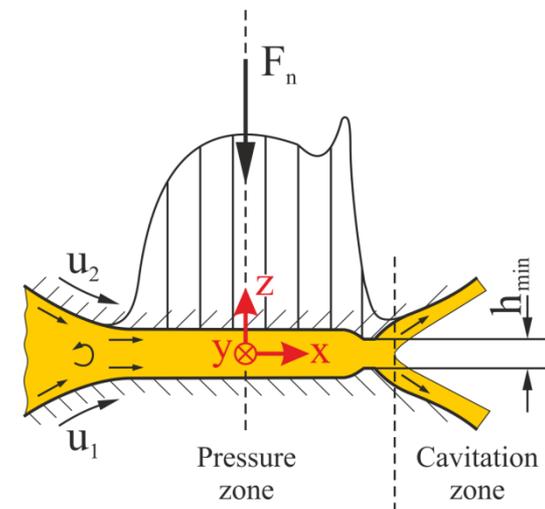
$$\frac{\partial}{\partial x} \left( \Phi_{xx}^p G_{1x} \frac{\partial p_h}{\partial x} \right) + \frac{\partial}{\partial y} \left( \Phi_{yy}^p G_{1y} \frac{\partial p_h}{\partial y} \right) = \frac{\partial}{\partial x} \left( \theta G_{2x} \frac{(u_2 - u_1)}{F_0} + \theta G_3 u_1 + \dots \right)$$

$$\theta G_3 \Phi_{xx}^s \frac{(u_2 - u_1)}{2h} + \frac{\partial}{\partial y} \left( \theta G_{2y} \frac{(v_2 - v_1)}{F_0} + \theta G_3 v_1 + \theta G_3 \Phi_{yy}^s \frac{(v_2 - v_1)}{2h} \right) + \frac{\partial}{\partial t} (\theta G_3)$$

with  $p_h > p_{cav}$  and  $\theta = 1$  in the pressure zone

$p_h = p_{cav}$  and  $\theta < 1$  in the cavitation zone

- applicable for any transient three-dimensional elastohydrodynamic contact
- mass-conserving cavitation algorithm
- variable density and viscosity along the x-, y- und z-axes



# 3D TEHL Calculation Model

## Calculation Model

Elastohydrodynamics

Real Gear Pair Geometry

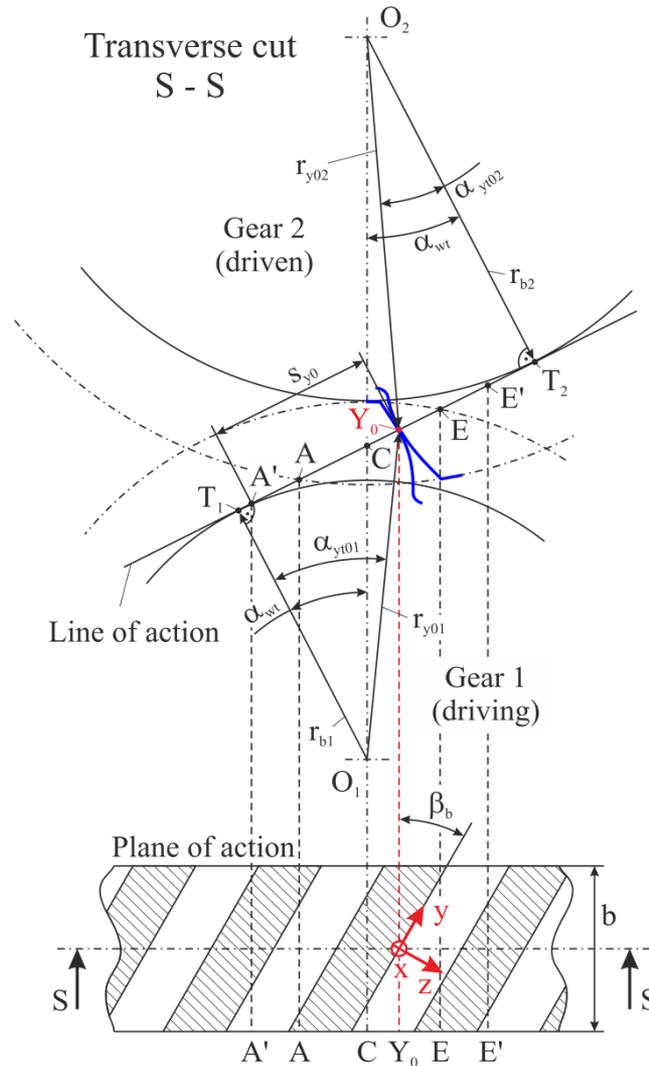
Realistic Load Distribution

Lubricant Rheology

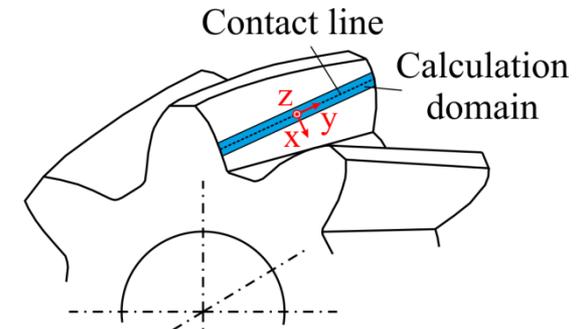
Rough Surfaces

Mixed Friction Conditions

Temperature Calculation



- local coordinate system centered in the contact point  $Y_0$  along contact line to consider gear geometry and gearing corrections
- line of action is defined in the center of the plane of action
- meshing takes place from point  $A'$  to point  $E'$
- consideration of realistic load distributions (RIKOR, LVR, FEM, ...)



# 3D TEHL Calculation Model

## Calculation Model

Elastohydrodynamics

Real Gear Pair Geometry

Realistic Load Distribution

Lubricant Rheology

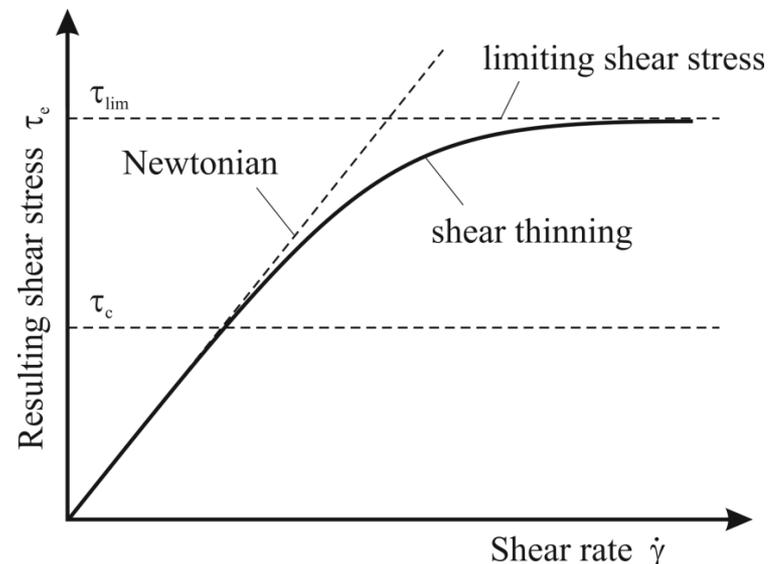
Rough Surfaces

Mixed Friction Conditions

Temperature Calculation

## Lubricant properties

- consideration of density, viscosity, thermal conductivity and specific heat capacity, dependent on local conditions in the calculation domain (temperature, pressure)
  - based on high pressure rheometer data
- non-Newtonian flow behavior including shear thinning and limiting shear stress
  - based on experimental traction data



# 3D TEHL Calculation Model

## Calculation Model

Elastohydrodynamics

Real Gear Pair Geometry

Realistic Load Distribution

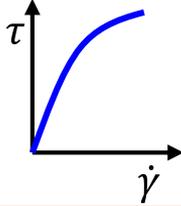
Lubricant Rheology

Rough Surfaces

Mixed Friction Conditions

Temperature Calculation

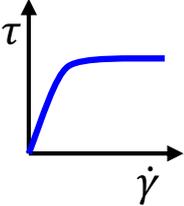
## Eyring

$$\dot{\gamma} = \frac{\tau_c}{\eta} \cdot \sinh\left(\frac{\tau}{\tau_c}\right)$$


+ specification of critical shear stress  $\tau_c$

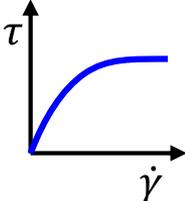
~~shear stress tends towards infinity~~

## Bair/Winer (simplified)

$$\dot{\gamma} = \frac{\tau}{\eta} \cdot \frac{1}{1 - \left(\frac{\tau}{\tau_{lim}}\right)^a}$$


+ specification of limiting shear stress  $\tau_{lim}$

~~nearly Newtonian behavior to  $\tau_{lim}$~~

$$\dot{\gamma} = \frac{\tau_c}{\eta} \cdot \sinh\left(\frac{\tau}{\tau_c}\right) \cdot \frac{1}{1 - \left(\frac{\tau}{\tau_{lim}}\right)^a}$$


➔ limiting shear stress is dependent on local pressure

# 3D TEHL Calculation Model

## Calculation Model

Elastohydrodynamics

Real Gear Pair Geometry

Realistic Load Distribution

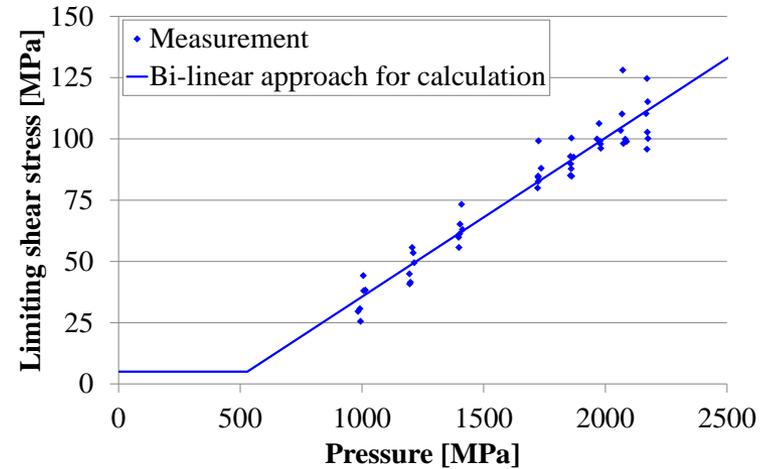
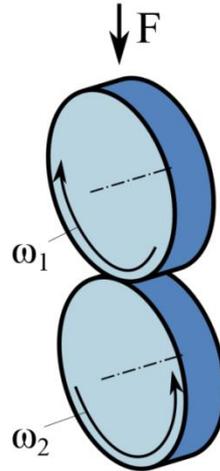
Lubricant Rheology

Rough Surfaces

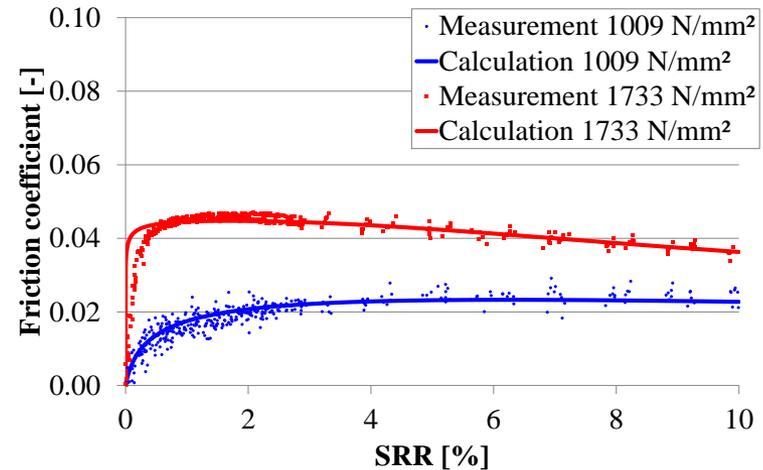
Mixed Friction Conditions

Temperature Calculation

## Twin-disk traction measurement – limiting shear stress



## Comparison of measured and calculated traction curves



Measurement data: IMKT, University Hannover, Germany

# 3D TEHL Calculation Model

## Calculation Model

Elastohydrodynamics

Real Gear Pair Geometry

Realistic Load Distribution

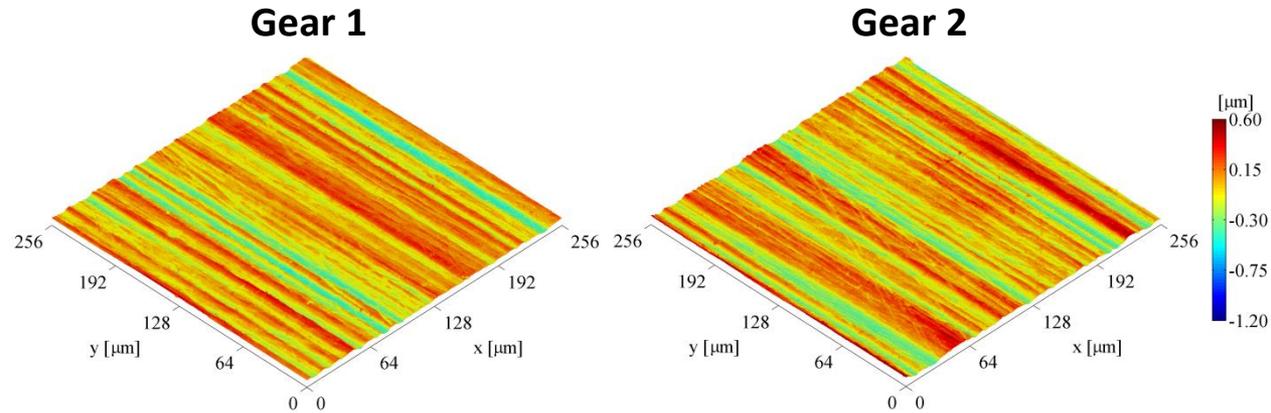
Lubricant Rheology

Rough Surfaces

Mixed Friction Conditions

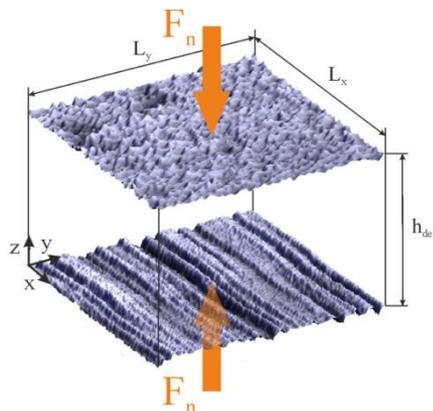
Temperature Calculation

## Measurement of real surface topographies of gear 1 and 2

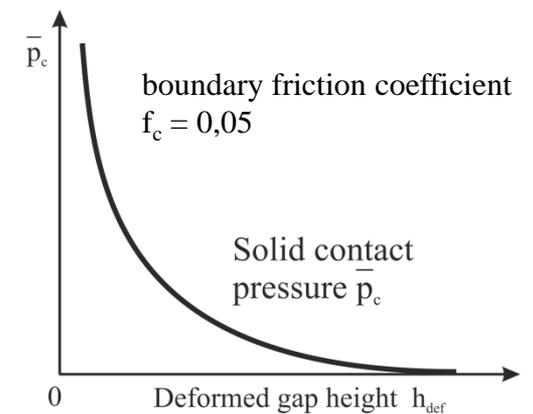


## Calculation of characteristic mixed friction maps

### Discrete solid contact model



### Characteristic map



# 3D TEHL Calculation Model

## Calculation Model

Elastohydrodynamics

Real Gear Pair Geometry

Realistic Load Distribution

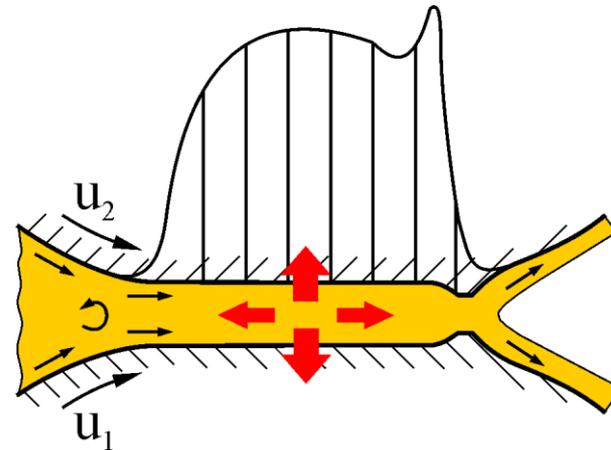
Lubricant Rheology

Rough Surfaces

Mixed Friction Conditions

Temperature Calculation

- consideration of compression, expansion, shear, convection and heat conduction by gap height resolved solution of the energy equation for the fluid
- coupling with Fourier heat equation for tooth flanks
  - definition of depth-dependent thermo-physical material properties allows the calculation of complex multi-layer coatings
- consideration of additional heat sources as a result of boundary friction in the transitional condition



# Content

---

- Introduction
- 3D TEHL Calculation Model
- Calculation Example
- Results
- Summary

# Calculation Example

## Geometry data and operating parameters

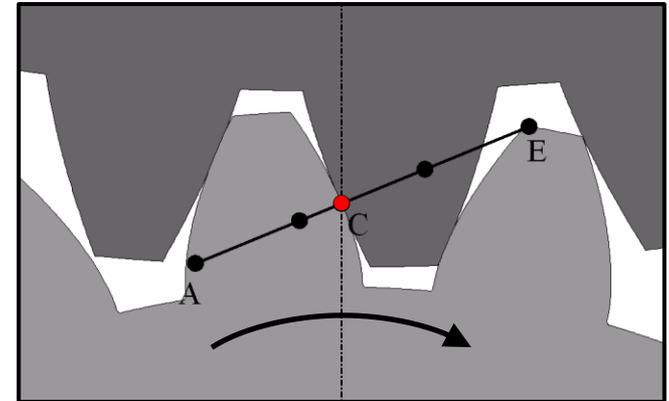
### Geometry data

- normal modulus:  $m_n = 3 \text{ mm}$
- normal pressure angle:  $\alpha_n = 20^\circ$
- helix angle:  $\beta = 20^\circ$
- number of teeth:  $z_1 = 24, z_2 = 61$
- center distance:  $a = 137 \text{ mm}$
- addendum modification:  $x_1 = 0.3125, x_2 = 0.1404$
- width of gear:  $b_1 = b_2 = 27.5 \text{ mm}$
- crowning:  $8 \mu\text{m}$
- tip relief:  $10 \mu\text{m} / 1.5 \text{ mm}$

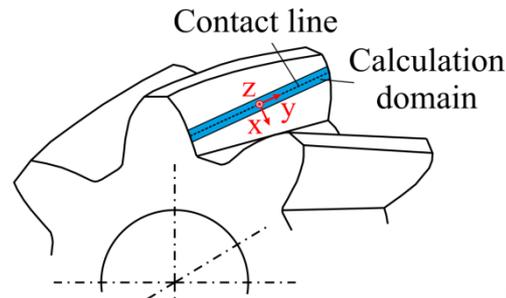
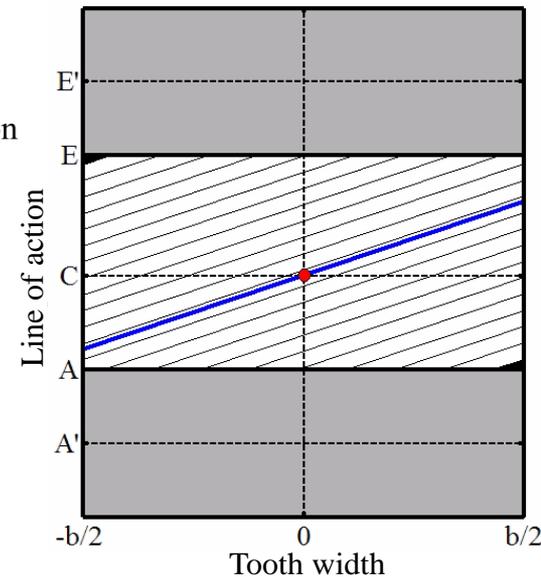
### Operating parameters

- torque:  $T_1 = 200 \text{ Nm}$
- speed:  $n_1 = 1485 \text{ min}^{-1}$
- power:  $P = 31.102 \text{ kW}$
- lubricant: ISO VG 150
- temperature (bulk, oil):  $60 \text{ }^\circ\text{C}$

### Meshing (center of plane of action)



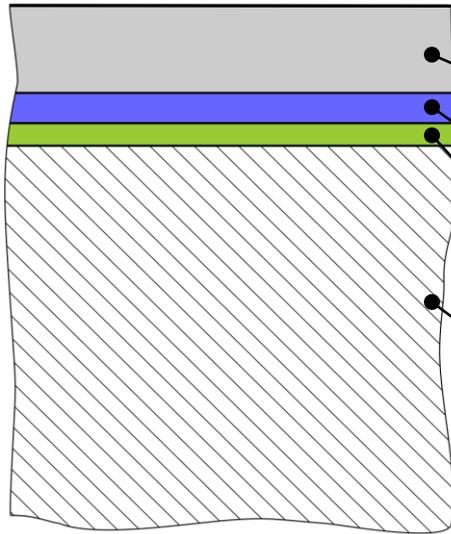
### Plane of action



# Calculation Example

## Coating

### Tooth flank coating structure



Layer	Thickness [μm]	Density [kg/m <sup>3</sup> ]	Heat conductivity [W/(m K)]	Specific heat capacity [J/(kg K)]
DLC coating a-C:H	2.7	1860	0.566	700
Tungsten carbide layer	0.82	15800	58	283
Chrome layer	0.53	7190	90	447
Substrate Steel 16MnCr5	-	7760	44	431

### Overview of calculation examples

Notation	Gear 1	Gear 2
St-St	uncoated steel	uncoated steel
St-DLC	uncoated steel	DLC coated steel
DLC-St	DLC coated steel	uncoated steel
DLC-DLC	DLC coated steel	DLC coated steel

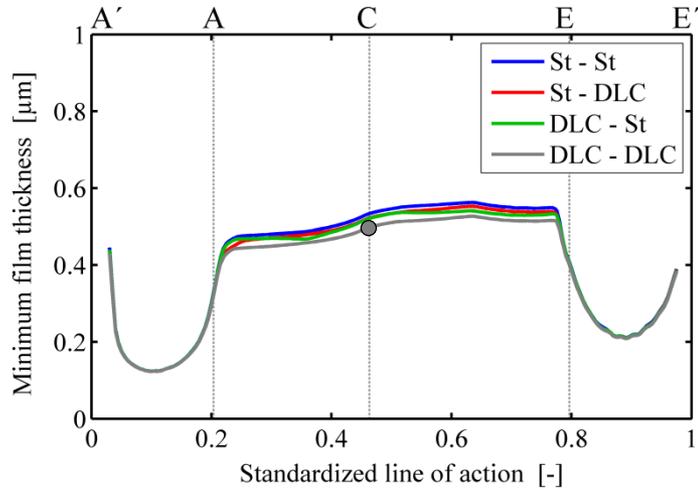
# Content

---

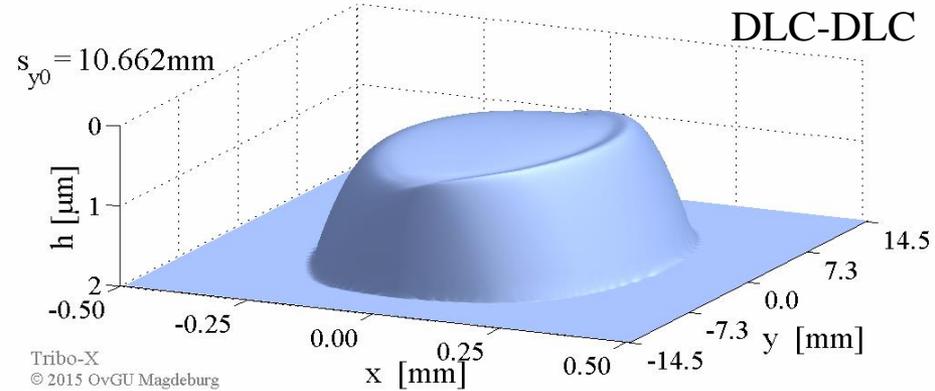
- Introduction
- 3D TEHL Calculation Model
- Calculation Example
- Results
- Summary

# Results

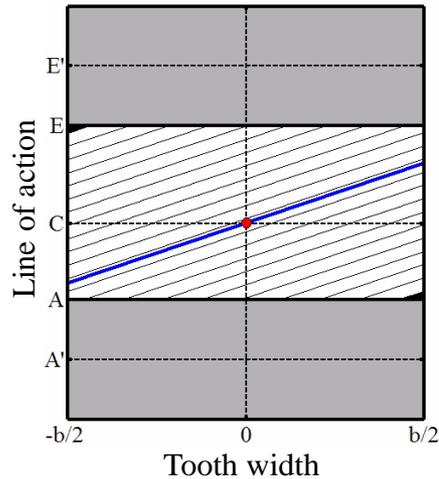
## Minimum film thickness



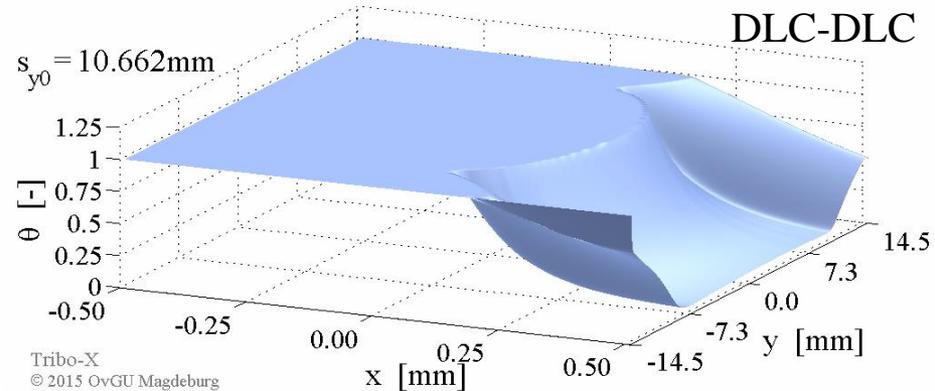
## Film thickness



## Plane of action

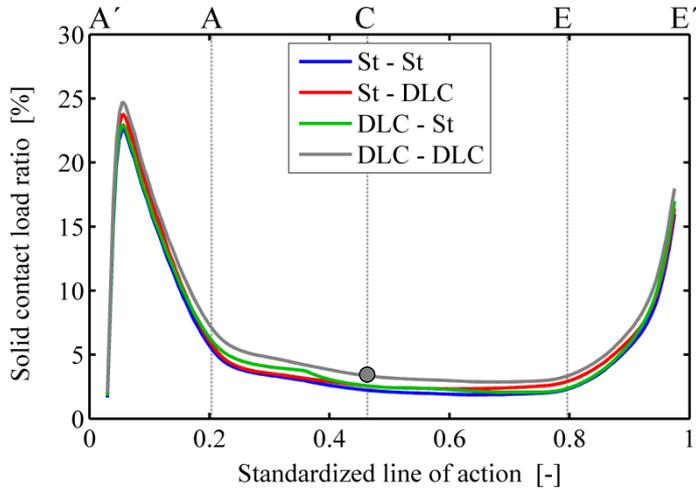


## Gap fill factor (cavitation)

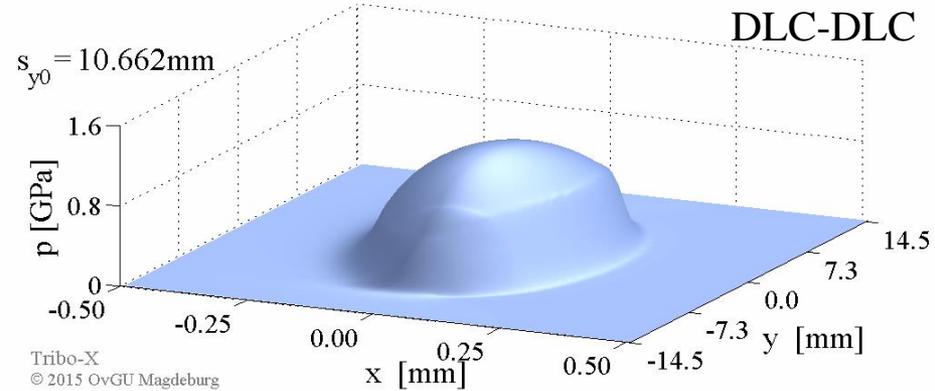


# Results

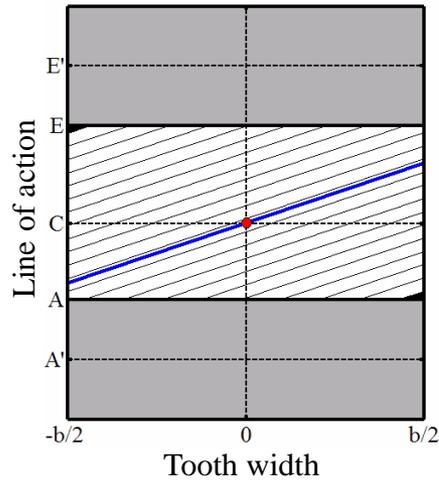
## Solid contact load ratio



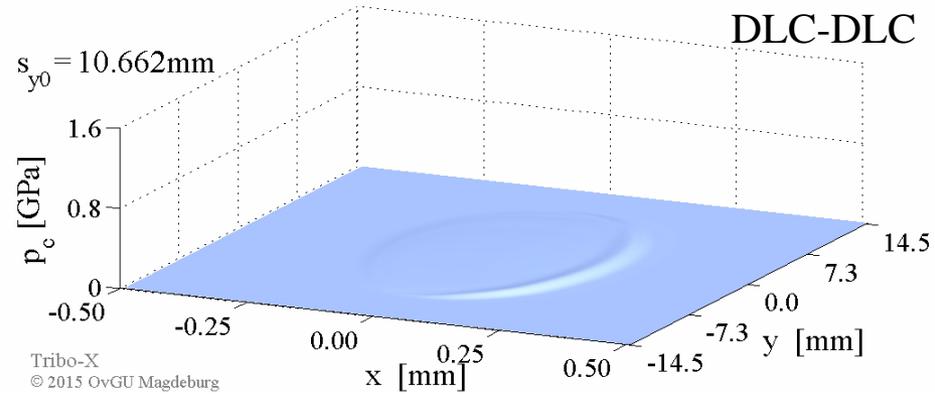
## Total pressure



## Plane of action

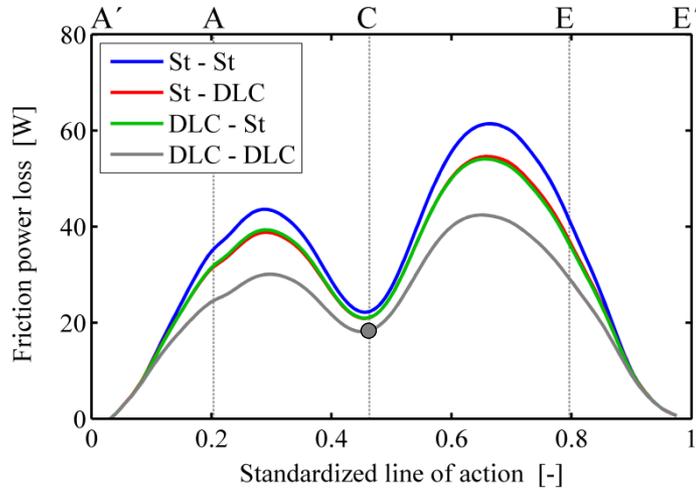


## Solid contact pressure

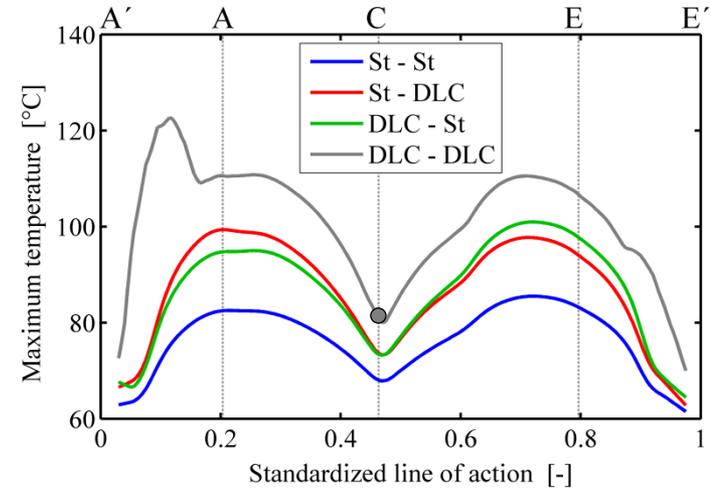


# Results

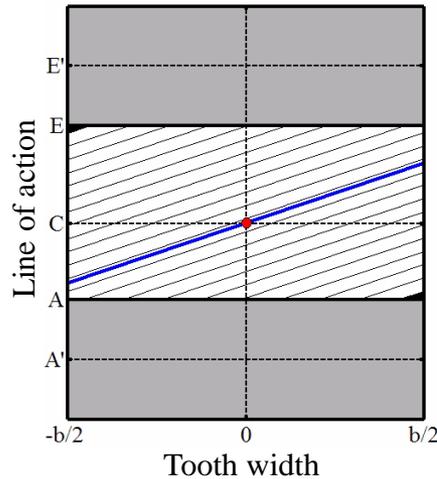
## Friction power loss



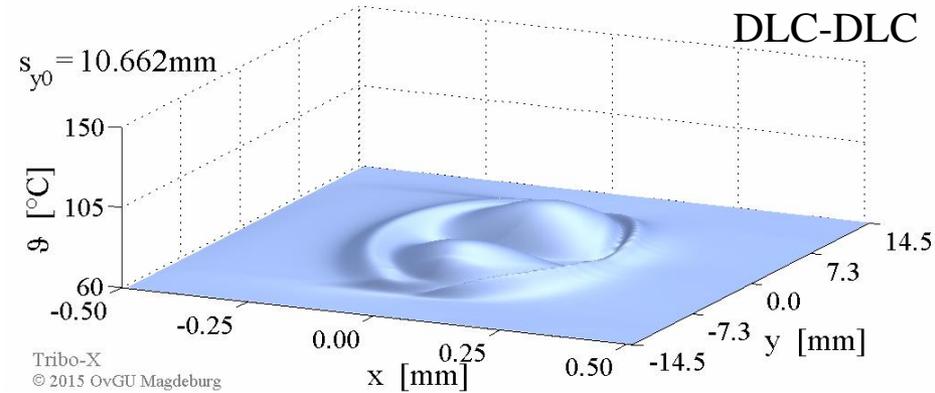
## Maximum temperature



## Plane of action



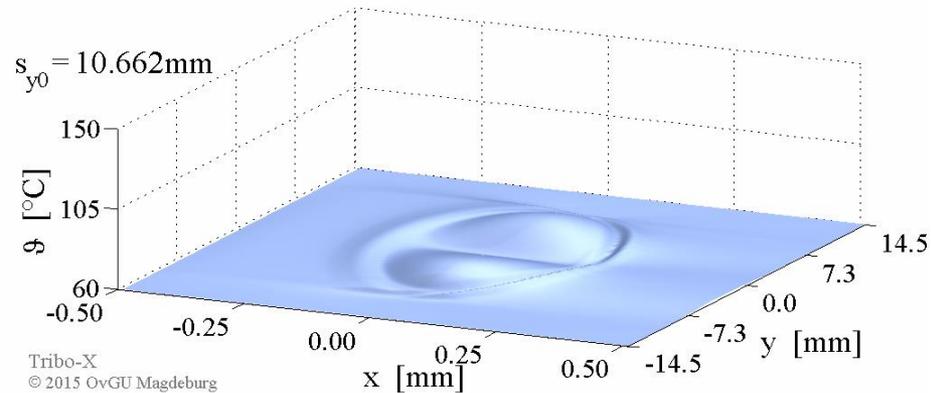
## Temperature (mid lubricating gap)



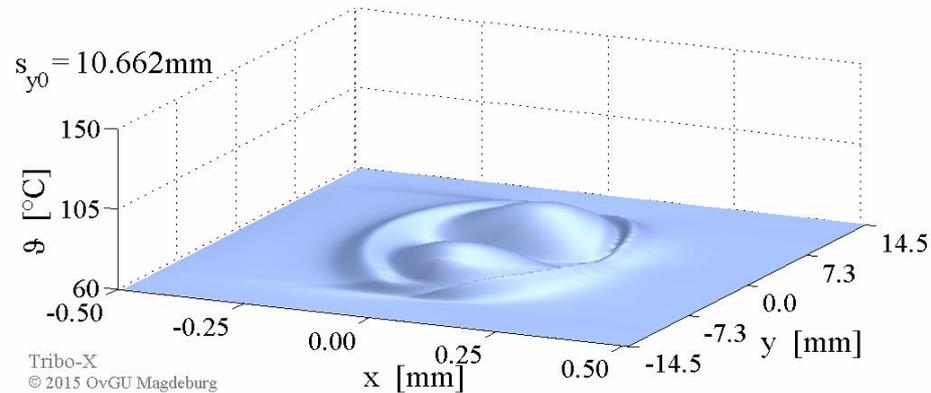
# Results

## Temperature (mid lubricating gap)

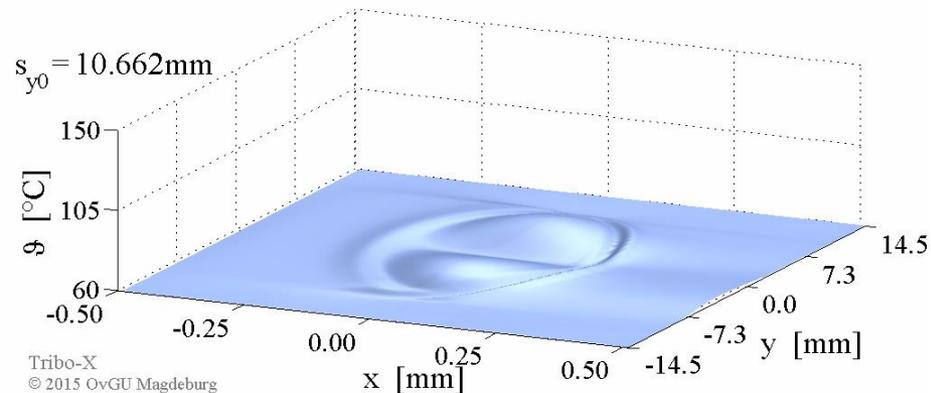
### DLC-St



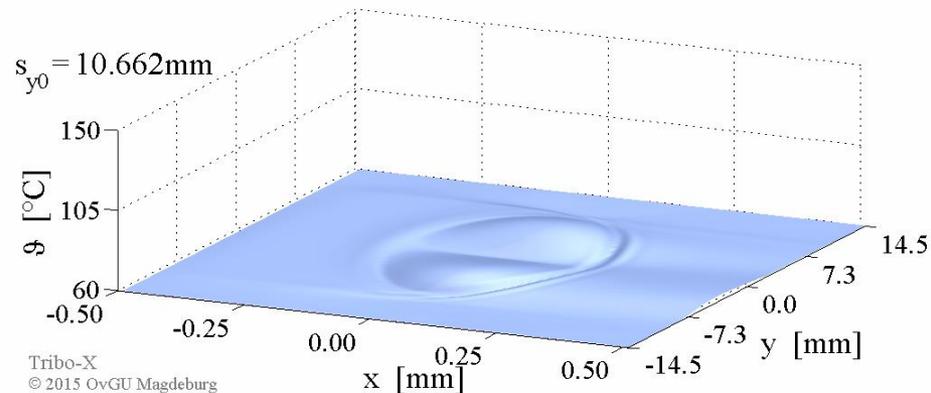
### DLC-DLC



### St-DLC

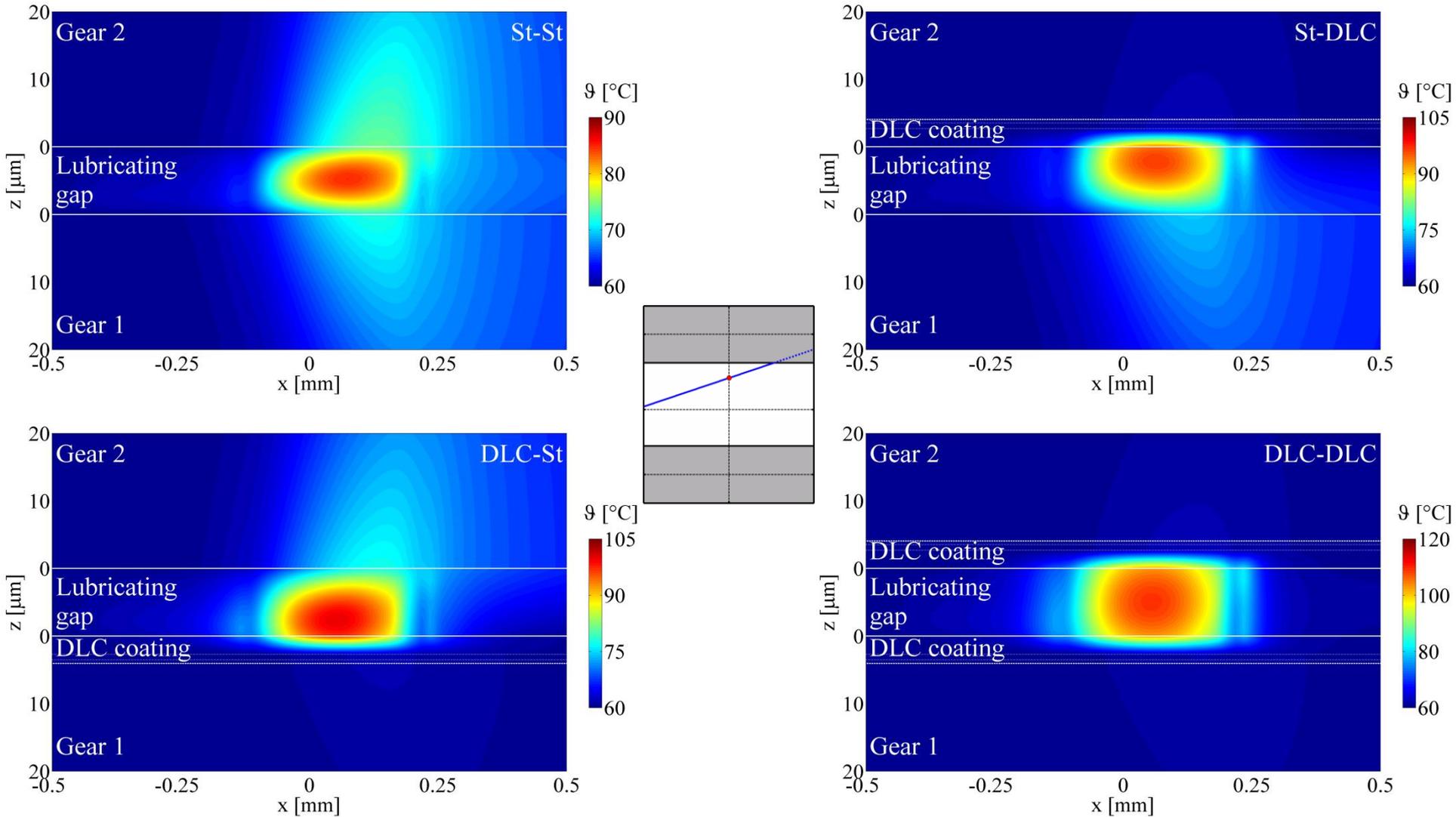


### St-St



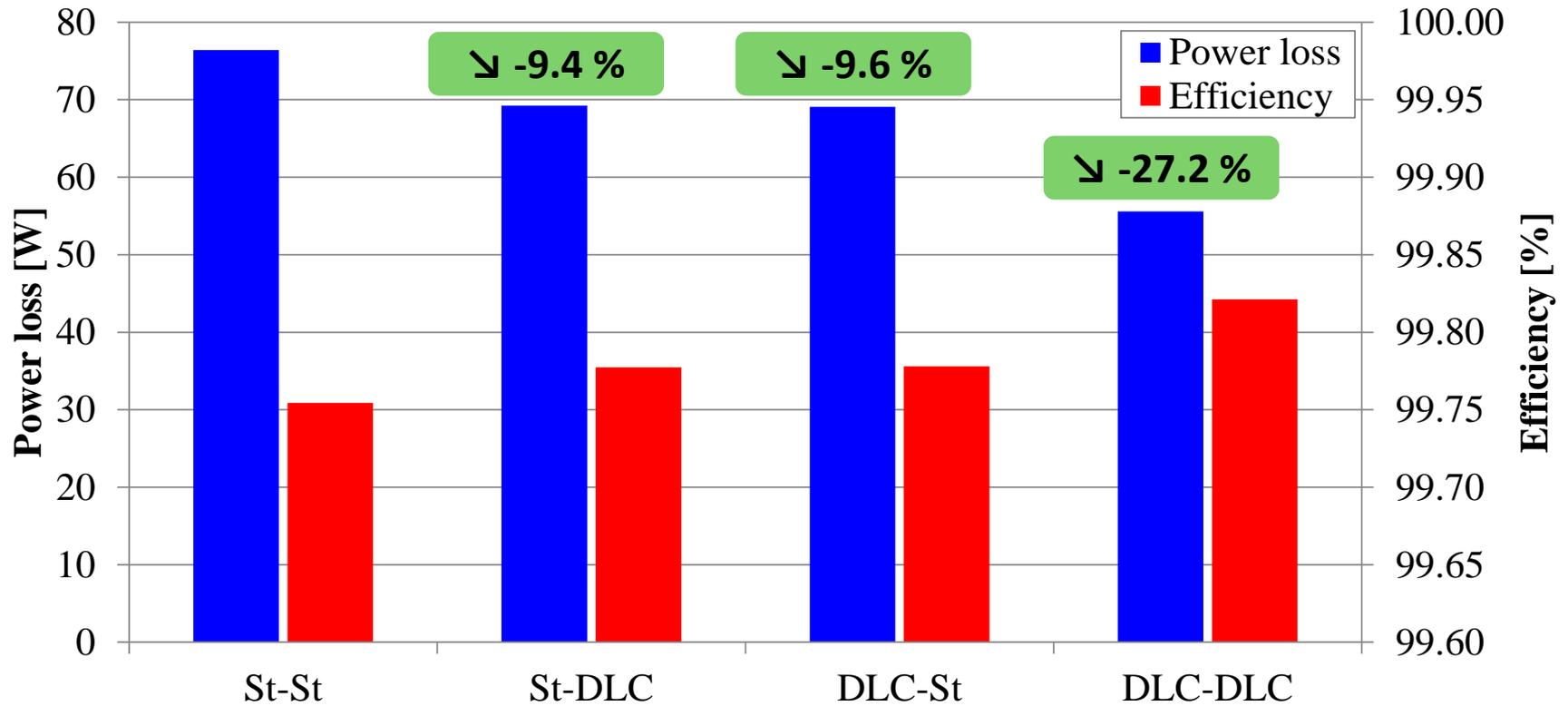
# Results

## Temperature distributions in sectional planes (center of gear, along line of action)

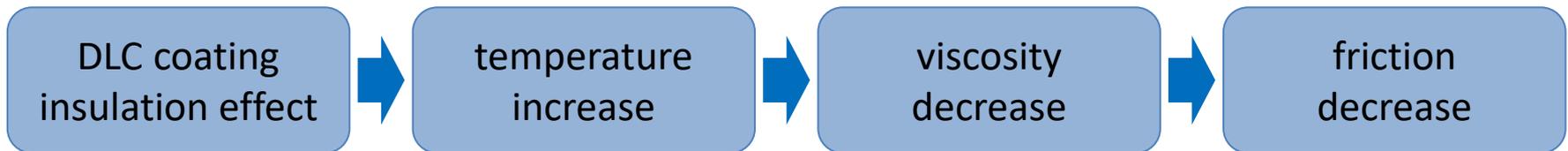


# Results

## Power loss and efficiency



### Causal chain



# Content

---

- Introduction
- 3D TEHL Calculation Model
- Calculation Example
- Results
- Summary

# Summary

- A calculation model for **transient thermal elastohydrodynamic simulation** was introduced.
  - applied on tooth flank contact of a helical gear pair
- Multi-layer **DLC coating** and realistic **rheological behavior** of the fluid were taken into account.
- DLC coated tooth flanks **reduced power loss** as a result of reduced hydrodynamic friction due to **higher temperatures**.
  - DLC coating on both gears led to highest temperatures and lowest power loss
- Higher temperatures in DLC coated contacts could be attributed to the **insulating effect** of the coating due to poorer thermal conductivity.
- Power loss results are **limited to mild mixed friction conditions**.
  - boundary friction coefficient of DLC coating may be different

# Contact & Acknowledgments



Otto von Guericke University Magdeburg  
Institute of Machine Design  
**Chair of Machine Elements and Tribology**  
Universitätsplatz 2  
39106 Magdeburg, Germany

Dipl.-Ing. Ronny Beilicke  
Phone: +49 391 67-52935  
E-mail: [ronny.beilicke@ovgu.de](mailto:ronny.beilicke@ovgu.de)  
Web: [www.imk-lmt.ovgu.de](http://www.imk-lmt.ovgu.de)

The results presented here were developed in part (flow model, high-pressure rheometry, twin-disk traction data) within the framework of the research project “Tribological Fluid Models” (FVV 1138).

The Joint Industrial Research (IGF) Project 17699 BG of the Research Association for Combustion Engines e.V. was funded through the German Federation of Industrial Research Associations (AiF) within the framework of the program to promote Joint Industrial Research by the Federal Ministry for Economic Affairs and Energy (BMWi) based on a decision by the German Bundestag.